

# Problem Solving: Work Backward

| Read and Understand  | Plan and Solve   | Check  |
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| Four students shared some mangoes for lunch, but 2 mangoes were too ripe to eat. The students cut up 4 mangoes, which made up $\frac{1}{3}$ of the mangoes that were left. How many mangoes were there in all? You need to find the number of mangoes the students started with. | Start with the number of mangoes the students cut up. Then work backward to find the original number of mangoes. These were $\frac{1}{3}$ of the mangoes left after the 2 ripe ones were thrown away. 4 mangoes are $\frac{1}{3}$ of 12. So there must have been 12 mangoes left after the ripe ones were discarded. Add the 2 overripe mangoes to the 12. The students started out with 14 mangoes. | Work forward to check your work. Start with 14 mangoes. Subtract the 2 overripe ones to get 12. One third of the 12 mangoes left is 4 mangoes, which is the number of mangoes the students cut up. |

Work backward to help you solve each exercise.

1. Phoebe played checkers with her sister. She won 4 times as many games as she lost. Phoebe won 12 games. If there were no ties, how many games did Phoebe play?

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2. Kim ordered a super-sized submarine sandwich and had it cut into equal pieces. She and 3 friends ate the same number of pieces.  $\frac{1}{4}$  of the sandwich was not eaten. For dinner that night, she ate 3 pieces, which were  $\frac{1}{2}$  of the leftovers. How many pieces were there originally?

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